## Linear Algebra

Programme(s) in which it is offered: B.Sc.B.Ed. Mathematics

| Course Category: Core | Schedule of Offering: Even |
| :--- | :--- |
| Course Credit Structure: 4 | Course Code: EG417 |
| Total Number of Hours: 5 | Contact Hours Per Week: 5 |
| Lecture: 3,3 | Tutorial: 1,2 |
| Practical: 0,0 | Medium of Instruction: English |
| Date of Revision: | Skill Focus: Others |
| Short Name of the Course: Linear Algebra | Course Stream |
| Grading Method: Regular | Repeatable: Credit |
| Course Level: Beginner |  |

## Course Description

This course is a core course for B.Sc. B.Ed. Mathematics students. This course discusses the fundamental theory of linear algebra.

## Course Introduction

This course is an introductory course in linear algebra - a study of vector (linear) spaces. The course discusses the theory of vector spaces, linear transformations and their significance. The course also to a certain extent relates branches of mathematics like Euclidean geometry, Matrix algebra and abstract algebra.

## Course Objective

The objectives of the course are:

1. To discuss the fundamental concepts of linear algebra
2. To expose the students to various tools of linear algebra
3. To study linear maps, their properties and applications
4. To study inner product spaces as generalisation of Euclidean spaces

## Course Outcome

At the end of the course students will be able to

1. Find the bases for a given vector space and vice versa
2. Determine the matrix of a given linear map and vice versa
3. Prove and apply the properties of linear maps
4. Apply the diagonalization process on suitable linear maps
5. Generalise certain properties of Euclidean geometry to inner product spaces

## PO-CO Mapping

<This should explain how the Course Outcomes (CO) are mapped with the Programme Outcomes (PO). All programmes to have two generic POs which can map to all minors/proficiency courses and foundation/self-immersion courses. Please tick the respective cells only; leave the other cells blank.>

PO-CO Mapping Matrix

| CO/PO Mapping | PO1 | PO2 | PO3 | PO4 | PO5 | PO6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| C01 |  |  |  |  |  |  |
| C02 |  |  |  |  |  |  |
| C03 |  |  |  |  |  |  |
| C04 |  |  |  |  |  |  |
| C05 |  |  |  |  |  |  |

## Prerequisites and other constraints

This course is offered to all students of B.Sc.B.Ed. Mathematics. There is no prerequisite course.

## Pedagogy

The teaching-learning of the course is organized through lectures, problem-solving sessions and student presentations.

## Suggested Reading:

1. Hoffmann and Kunze (1998). Linear Algebra, Second Ed. Prentice Hall of India New Delhi.
2. Kumaresan (1999). Linear Algebra: A Geometric Approach. Prentice Hall of India, New Delhi.
3. Herstein (2006). Topics in Algebra. Wiley.
4. Lang (1986). Introduction to Linear Algebra, Second Ed. Springer-Verlag. New York.
5. Friedberg, Insel, and Spence (2009). Linear Algebra, Fourth Edition. PHI.

## Evaluation Pattern

Evaluation Matrix

| Continuous Internal Assessment (CIA) <br> Components* | Component Type | Weightage Percentage | Total Marks | Tentative Dates | Course <br> Outcome <br> Mapping |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mid-semester exam | 50\% of CIA | 30 | Around $9^{\text {th }}$ week | 1, 2, 3 |
|  | Assignment | 25\% of CIA | 15 | End of each module | 1, 2, 3, 4, 5 |
|  | Quizzes/Problem Solving | 17\% of CIA | 10 | Every two weeks | 1, 2, 3, 4 |
|  | Presentations | 8\% of CIA | 5 | End of two modules | 1, 2, 3, 4, 5 |
|  | CIA Marks | 100\% of CIA | 60 |  |  |
| ESE |  | 40\% | 100 | End of the semester | 1, 2, 3, 4, 5 |

## Module Sessions

## Module 1: Vector Spaces

Vector spaces, Subspaces, Linear Combinations, Linear span, Linear dependence and Linear independence of vectors, Basis and Dimension, Finite dimensional vector space - some properties. Quotient spaces, Direct sums.

## Reading:

1. Kumaresan
2. Friedberg
3. Hoffman

Activities:
a. Quiz
b. Assignment

## Module 2: Linear Maps - I

Linear maps, Matrices of Linear maps, Change of basis and the effect on associated matrices, Kernel and Image of a linear transformation, Rank-Nullity theorem and applications.

## Reading:

1. Friedberg
2. Kumaresan

## Activities:

a. Quiz
b. Assignment
c. Presentation

## Module 3: Linear Maps - II

Singular and non-singular linear transformations, Elementary matrices and transformations, Similarity, Eigen values and Eigen vectors, Diagonalisation, Characteristic polynomial, Cayley - Hamilton Theorem, Minimal Polynomial.

## Reading:

1. Friedberg
2. Hoffman
3. Kumaresan

## Activities:

a. Quiz
b. Assignment

## Module 4: Inner-product Spaces

Inner product spaces, Euclidean spaces, Distance, Length, Properties, Parallelogram Law, Cauchy-Schwarz inequality, Orthogonal and Orthonormal vectors, Gram-Schmidt Orthogonalisation Process, Orthogonal complement.

## Reading:

1. Kumaresan
2. Friedberg

## Activities:

a. Quiz
b. Assignment
c. Presentation

